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Modelling of Maximum Temperature Forecasting by Arima Method in the Boeny Region of Madagascar

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Abstract: *The study area is the BOENY region, delimited in latitude between 15° South and 18° South and in longitude between 44° East and 48° East.*

We modeled the maximum temperature from the year 1979 to 2018 by the ARIMA method. The study leads us that the data follow Gauss's law. According to this method, on average the values of the annual maximum temperature are between 27.8°C and 28.6°C. The year 1984 is the less hot year, the temperature is 27.52°C. The hottest year is 2028 with a value of 28.95 °C.

Keywords: *Temperature, forecast, ARIMA, Boeny region.*

I. Introduction

The threat of climate change is the focus of international concern. In order to understand this international problem, knowledge of the meaning of the term 'climate change' is necessary. The meaning of the term 'climate change' is fairly straightforward and no longer controversial. However, its causes, magnitude and impacts on human well-being and the environment are much debated.

In Madagascar, the impact of climate change, particularly temperatures, remains a major concern for the Big Island. It is likely to hit the entire country hard in the coming years.

It is for this reason that this study leads us to model the annual average value of the maximum temperature by the ARIMA method. In this respect, the proposal of a model of the medium-term forecast in a study area is one of the most important steps in conducting this study.

II. Material and Methods

2.1 Presentation of the study area

The study area (see Figure 1) is between latitude 15°South and 18°South and longitude 44° East and 48° East.

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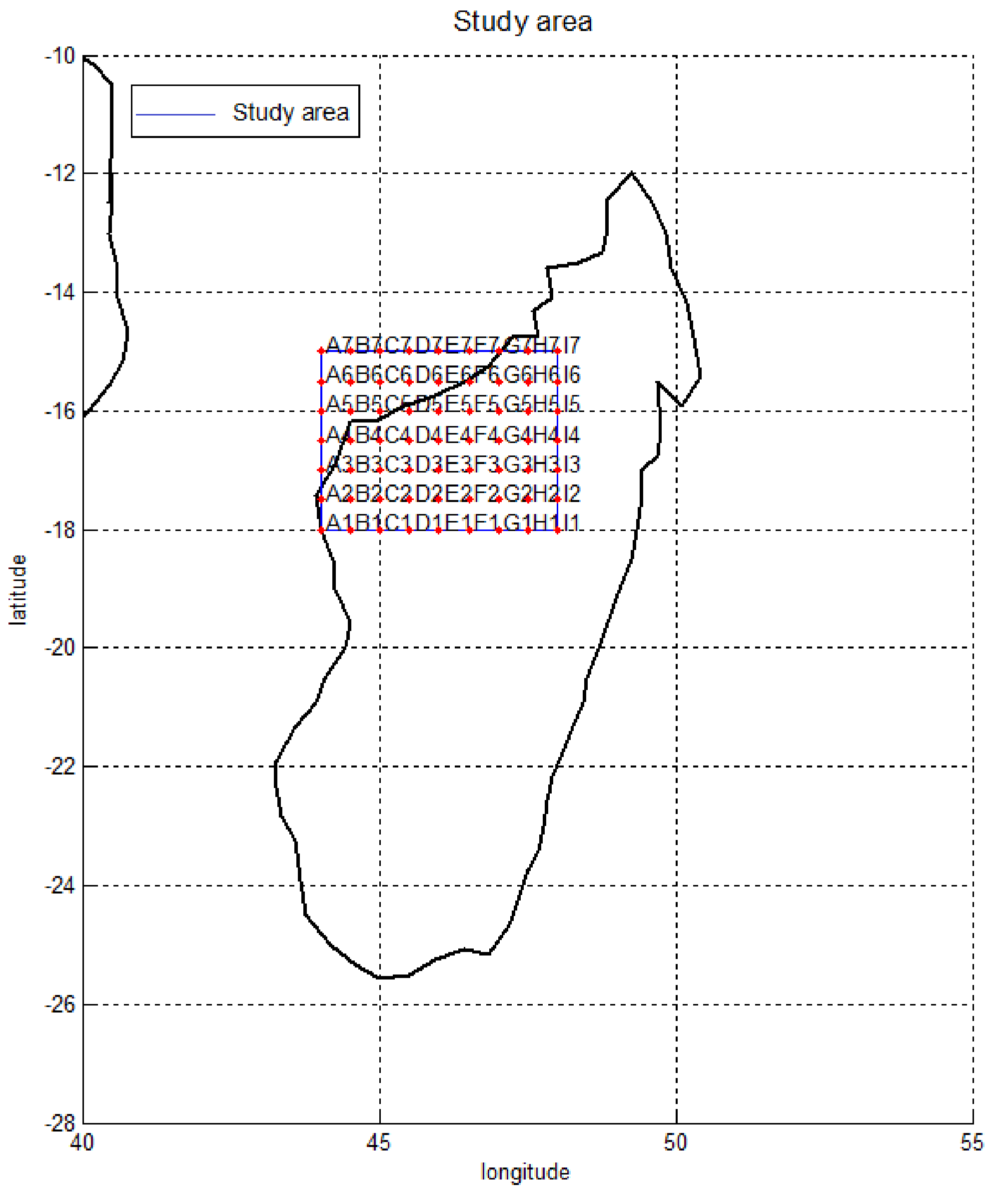

Figure 1 : Study area 44° ≤ longitude ≤ 48° and -18° ≤ latitude ≤ -15°

2.2 Databases

The meteorological data we used are from the daily reanalysis data of the European Centre for Medium range Weather Forecasts (ECMWF) experiment (ERA5) at synoptic scale with a 0.5° x 0.5° grid of maximum temperature over a time depth covering the period 1979-2018.

2.3 ARIMA modelling [1] [2] [3] [4] [5] [6] [7] [8]

Definition: We will say that $X = (X_t)$ is an $ARIMA\ (p, d, q)$ process, if there exists a natural number d such that the process $Y_t = (1 - B)^{\ d} Xt$ is an $ARMA(p, q)$. In other words, there exist two polynomials $A(z)$ and $C(z)$ of degree p and q respectively and a white noise (ε_t) defined on the same $(\Omega, Q, P\ )$ such that:

$(1 - B)^d\ A(B)X_t = C(B)\varepsilon_t$

With the code:

- $e\ <-rnorm(200),$
- $Marchealeatoire\ <-cumsum(e),$
- $ts.plot(Marchealeatoire, type = "l", col = "blue"),$
- $abline(0,0, col = "red"),$

- $acf(Marchealeatoire, 20, "correlation")$.

We obtain the trajectory of $X_t = X_{t-1} + \varepsilon_t$ and its autocorrelation function.

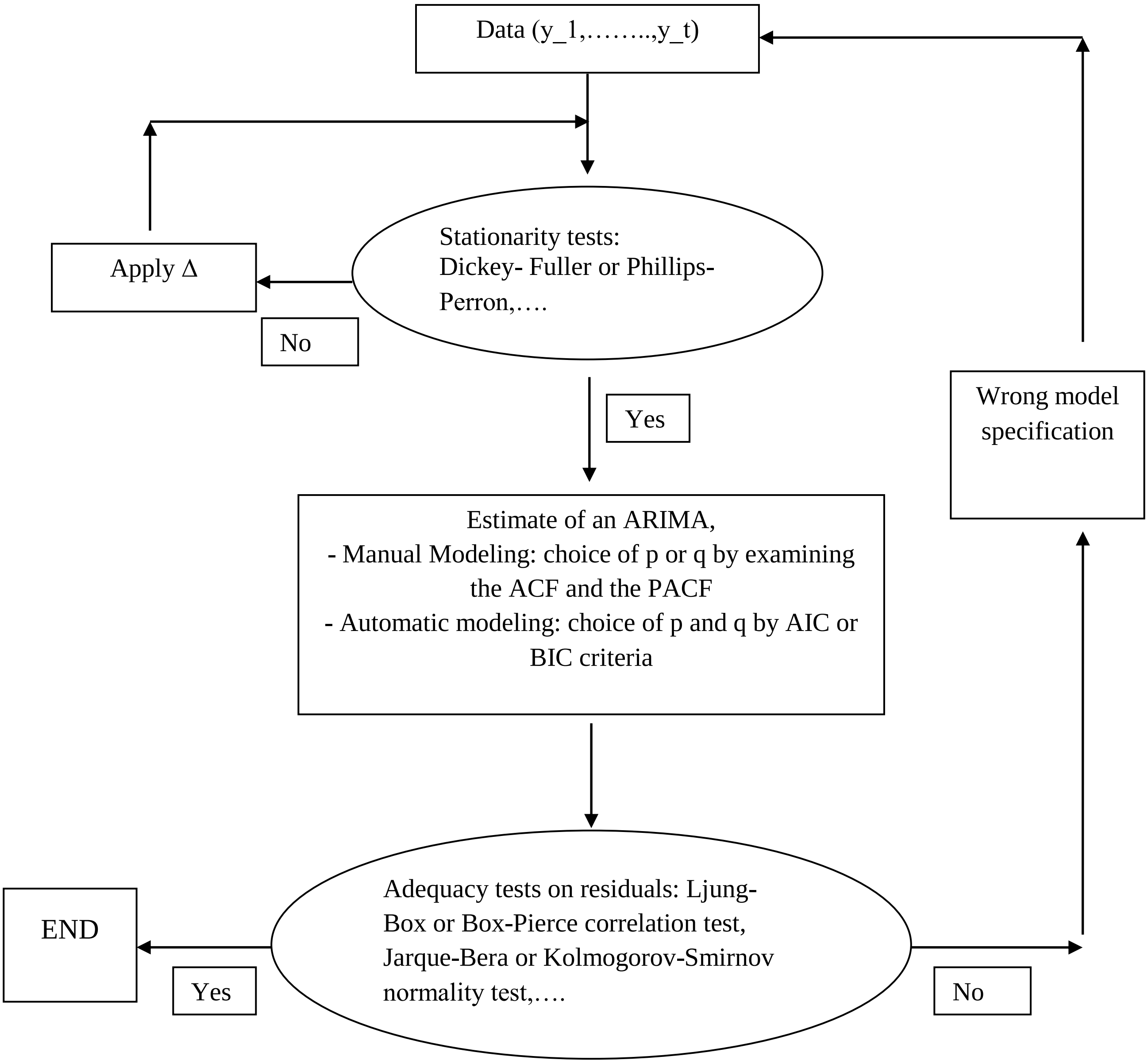

Figure 2: General diagram of the modelling of a time series by an ARIMA model

2.3.1 Modelling steps

Stationarisation by differentiation

- The differentiation operator Δ = 1 − B, (or Δ^d) removes trends, d is estimated by performing stationarity tests on the raw series and then on the residual series. An estimator of d is the total number of times stationarity is rejected.

The residual series assumed to be stationary will be modelled by an ARMA (p, q).

Estimation

- R offers the possibility of using two methods:
- the maximum likelihood method "ML",
- and the conditional least squares method "CSS".

Validation

- Is the selected model compatible?

We carry out suitability tests on the residuals: absence of autocorrelation, normality, homoscedasticity,...

2.3.2 Non-stationarity test

Augmented Dickey and Fuller test:

Robust to autocorrelation compared to the Dickey-Fuller test

$$\begin{cases} H_0 : y_t \sim I(1) \\ H_1 : y_t \ n'estpas \ I(1) \end{cases}$$

We run the regression

$$\Delta y_t = \beta' D_t + \pi y_{t-1} + \sum_{j=1}^{p} \psi_j \Delta y_{t_j} + u_t$$

$$ADF = T\hat{\pi} \frac{T\hat{\pi}}{(1-\widehat{\psi_1}-\cdots-\widehat{\psi_p}}$$

Phillips-Perron test

Robust to heteroscedasticity

We run the regression:

$$\Delta y_t = \beta' D_t + \pi y_{t-1} + u_t$$

$$PP = T\hat{\pi} - \frac{1}{2} T^2 \frac{SE(\hat{\pi})}{\hat{\sigma}^2} (\hat{\lambda}^2 - \hat{\sigma}^2)$$

Where $\hat{\sigma} = \frac{1}{T-k} \sum_{i=}^{T} \hat{u}_t^2 \hat{u}_t$: residuals of the regression;

$SE(\hat{\pi}) = écart - type \ de \ \hat{\pi}$;

$\hat{\lambda}^2 = \hat{\sigma}^2 + 2 \sum_{j=1}^{q} \left(1 - \frac{j}{q+1}\right) \hat{\gamma}(j), (Newey - West),$

$\hat{\gamma}(j) = \frac{1}{T} \sum_{i=j+1}^{T} \hat{u}_t \hat{u}_{t-j}.$

2.3.3 Estimation:

With the code: $fit7 \ <- arima0(ari, order \ = \ c(1,1,0), method = "ML"), fit7$ on we get

$Call : \ arima0(x \ = \ ari, order \ = \ c(1,1,0), method \ = \ "ML")$

Coefficients :

$ar1$

0.6714

$s.e. 0.0368$

$sigma\hat{}2 \ estimated \ as \ 0.9678 : \ log \ likelihood \ = \ -561.32, \ aic \ = \ 1126.64$

Note: The estimation of the model appears to be of good quality, as the estimator of a_1 is very close to the true value.

2.3.4 Suitability tests:

With the code: $Box.test(fit7\$residuals, lag \ = \ 10, type \ = \ "Box - Pierce")$ we obtain :

Box-Pierce test

data : fit7$residuals

X-squared = 8.728, df = 10, p - value = 0.5581

The p-value is large so the residuals are not correlated.

With the code: $library(nortest), lillie.test(fit7\$residuals)$ we get

$Lilliefors \ (Kolmogorov - Smirnov) \ normality \ test$

$data : \ fit7\$residuals \quad D \ = \ 0.0407, p - value \ = \ 0.1114$

So the data follow a Gaussian distribution.

III. Results and discussion

3.2.5 Graphical representation of the model

Figures 3 and 4 show the predictions of the annual mean maximum temperature observed during the study period. The curves of the observation data in purple and the curves in red are the forecast models. The forecast values of the annual mean maximum temperature for the years 2019 to 2028 are shown in Table 1.

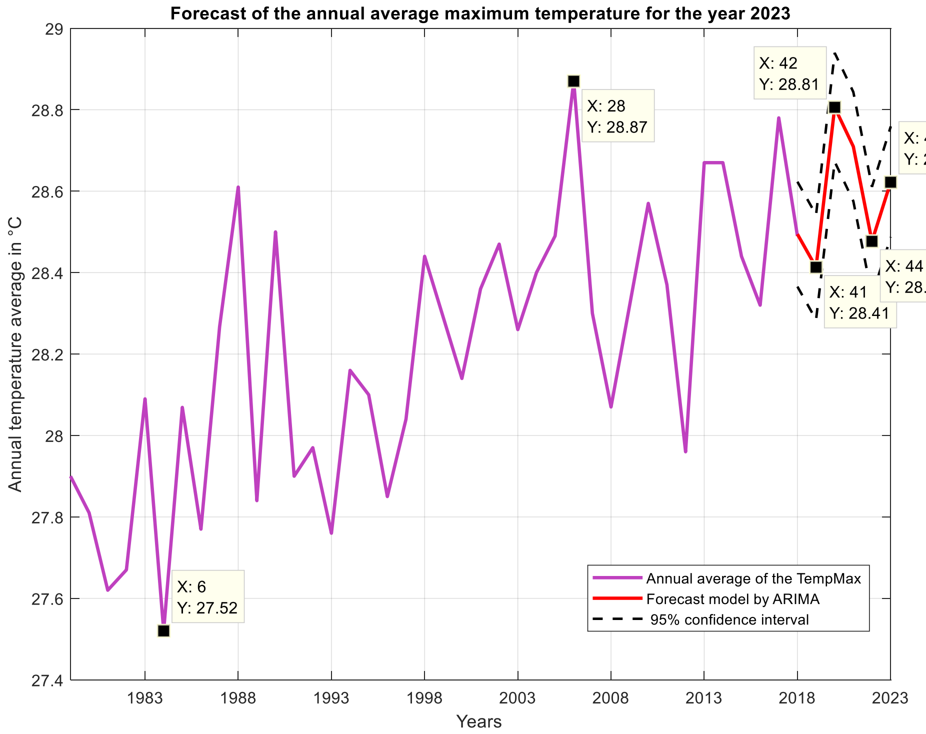

Figure 3: Forecast curve for maximum temperature in 2023

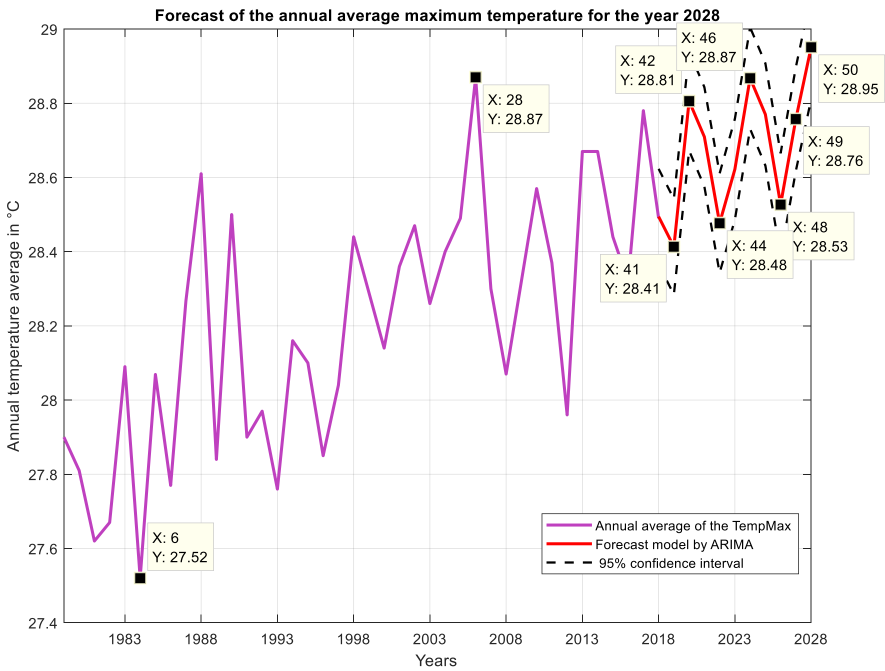

Figure 4: Forecast curve for maximum temperature in 2028

Table 1: Forecast of annual average maximum temperature by the ARIMA method

Years of the forecast	Values of the annual average temperature in [°C]
2019	28.41
2020	28.81
2021	28.71
2022	28.48
2023	28.62
2024	28.87
2025	28.77
2026	28.53
2027	28.76
2028	28.98

Analysing the curves, the average values of the maximum temperature range from 27.8 °C to 28.6 °C. The minimum value is 27.52 °C (in 1984) and the maximum value is 28.95 °C (in 2028).

IV. Conclusion

In this article, we are interested in the quantitative analysis of the daily maximum temperature from 1979 to 2018 in the Boeny region of Madagascar. This part is located between longitude 44° East and 48° East, latitude 18° South and 15° South. To study the predictability of these parameters, it is necessary to make a quantitative study of some climatological parameters. In our case, we proceeded to the use of statistical methods, the ARIMA method.

According to the ARIMA method, the models retained for the average values of the maximum temperature are between 27.8 °C and 28.6 °C. The year 1984 is the least temperate year, the temperature value is 27.52 °C. The most temperate year is the year 2028 with a temperature value of 28.95 °C.

V. References

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